

Folding domain B of protein A on a dynamically partitioned free energy landscape

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The B domain of staphylococcal protein A (BdpA) is a small helical protein that has been studied intensively in kinetics experiments and detailed computer simulations that include explicit water. The simulations indicate that BdpA needs to reorganize in crossing the transition barrier to facilitate folding its C-terminal helix (H3) onto the nucleus formed from helices H1 and H2. This process suggests frustration between two partially ordered forms of the protein, but recent ϕ value measurements indicate that the transition structure is relatively constant over a broad range of temperatures. Here we develop a simplistic model to investigate the folding transition in which properties of the free energy landscape can be quantitatively compared with experimental data. The model is a continuation of the Muñoz–Eaton model to include the intermittency of contacts between structured parts of the protein, and the results compare variations in the landscape with denaturant and temperature to ϕ value measurements and chevron plots of the kinetic rates. The topography of the model landscape (in particular, the feature of frustration) is consistent with detailed simulations even though variations in the ϕ values are close to measured values. The transition barrier is smaller than indicated by the chevron data, but it agrees in order of magnitude with a similar α -carbon type of model. Discrepancies with the chevron plots are investigated from the point of view of solvent effects, and an approach is suggested to account for solvent participation in the model.

folding landscape | frustration | protein folding

The routes a protein travels on the way to its native ensemble are the result of a sensitive exchange between energy and entropy coupling the protein to its solvent environment. Often the basic topography of the folding landscape (1) can be understood just from what would be necessary kinetically for a protein-like molecule to organize itself into a particular native shape (2–4), but the detailed way in which a protein interacts with solvent can qualitatively affect the way it folds (5, 6). The conformation of a protein is coupled to large-scale fluctuations in solvent density (7–9), and for small globular proteins investigated in kinetics experiments, most of the change in solvent exposure (10) can occur before the protein is half folded. The rate at which a protein explores its conformational space is slaved to local solvent motions (11, 12), and together these effects can have a significant influence on the time scale for folding.

Recently methods have become available to simulate proteins with explicit solvent on a time scale long enough to explore folding (13–15). These simulations provide the most precise picture of protein kinetics, but are as a result less wieldy to describe variations that occur across different experiments and solvent conditions (16–18). Typically, much more simplistic α -carbon type models have been used to address these problems, and when guided by experiment they can provide an accurate description of the interplay among protein folding routes (3, 4). A parallel approach established by Muñoz and Eaton (19–21) is to partition the free energy landscape of the protein into a network of small ensembles that can be described by polymer physics methods. This approach has the advantage that solvent effects might be included on a practical time scale, but it is usually less accurate than explicit chain models because the partitioning methods introduce dynamical

constraints that conflict with, or oversimplify, the kinetics of the protein (22, 23). Here we develop a method to solve this problem.

In the Muñoz–Eaton model, the configuration space of a protein is in effect partitioned in terms of a local order parameter describing the proximity of chemical bond angles in the residues to their native values. The partitioning is accomplished by labeling the residues in a protein configuration as folded (native like) or unfolded (free, or ensemble like) depending on their order parameter values, and then grouping together configurations that have the same pattern of labels. Configurations with unfolded loops (24, 25) are neglected in the model so that folded segments always represent independent nuclei, and consequently the ensemble free energies are simple to describe. The model can be solved exactly by special techniques (26, 27), and it provides a convenient way to construct basic inferences from experiments (28, 29). Nevertheless, the terms that are being neglected (unfolded loops and intermittency of native contacts between folded segments (30, 31)) are precisely those that coordinate the expulsion of solvent from the protein (2, 13, 32), and it is of interest to describe these terms from the point of view of the original model.

We accomplish this here by continuing the geometric approach of Muñoz and Eaton, including separate order variables to describe the state of contact between the folded segments. The resulting system of constraints resembles the local-order coupling model for explicit chains (33). To test the model, we use it to describe the folding landscape of the B domain of staphylococcal protein A (BdpA), which allows an extensive comparison to thermodynamics and kinetics measurements. BdpA (Fig. 1) is one of the most widely studied proteins of the past decade (34). Folding kinetics and single-molecule FRET measurements indicate that BdpA folds cooperatively over a broad range of solvent conditions (18), yet the system is still small enough to simulate by first principles methods on a computer (13–15). The folding nucleus (16), which forms around the first two helices, includes most of the binding interface from the complex with an IgG Fc fragment (35); H3 is unstructured in the complex, but structured in the transition state in all-atom simulations; however, in crossing the transition barrier, further rearrangement of the helices is required to consolidate contacts with H3 before the protein can fold. These features suggest that BdpA is weakly frustrated by extra “functional” requirements (binding preferences) of *Staphylococcus aureus* (34). But recent measurements to detect temperature changes in the transition structure (17) indicate that whatever frustration exists, it is not strong enough to divide the landscape into kinetically separate routes (29). By fitting our model to thermodynamic stability data (17, 29) we are able to bridge between the kinetics measurements

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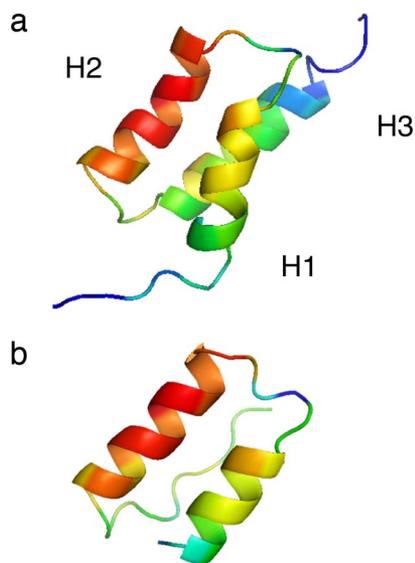


Fig. 1. Native structures of BdpA. (a) NMR structure of wild-type BdpA colored according to ϕ values calculated later in this work. ϕ values in the range $0 \leq \phi \leq 0.8$ correspond to blue, green, yellow, orange, and red. (b) Crystal structure from the complex of BdpA with the IgG Fc fragment colored as in a.

and the detailed simulations to describe the folding landscape under various solvent conditions.

Model

We consider systems that can be described by a $G\bar{o}$ (native only) interaction model in which nonnative contact is repulsive at short distances just to exclude the volume occupied by the protein (3, 4).

Let $q_i = 0, 1$ label the local structure of a residue i (folded or unfolded) in a partially unfolded protein as in the Muñoz–Eaton model. Each pattern of labels $\{q_i\}$ describes an ensemble of protein configurations Γ with structurally similar folded segments α_k . To describe the intermittency of contacts between the α_k , we partition Γ into smaller ensembles $\Gamma_n \in \Gamma$ according to whether the degree of native organization between pairs of folded segments α_k and α_l exceeds some threshold value. This is accomplished by providing the folded segments with separate labels (superscripts), $\alpha_k \rightarrow \alpha_k^a$, so that native contact between two segments α_k^a and α_l^b is established only if $a = b$. Leaving to later the question of what actually decides the threshold values for native order, the ensembles Γ_n can each be depicted by a Feynman-like diagram (36) formed by the following procedure [see supporting information (SI) Fig. 5]: First a line is drawn to represent the unfolded protein and labeled circles are placed at points along its length to represent the α_k^a . Circles with the same label are then joined together into nuclei by bending the unfolded lines to form the diagram (note that two circles can have the same label only if contacts exist between them in the native state). Each Γ contains an ensemble Γ_1 corresponding to the fully collapsed (natively connected) configuration of the α_k^a , and each partially collapsed diagram $\Gamma_{n \neq 1}$ corresponds to a topologically different way of “pulling apart” the folded segments in Γ_1 . For small proteins like BdpA, there is no need to consider diagrams with more than four folded segments, so the number of diagrams in Γ is always ≤ 15 .

To describe the free energy of a diagram the energy is then defined as $E = -\varepsilon \sum_{i < j} Q_{ij}(\Gamma_n)$, where ε is the energy per contact, $Q_{ij}(\Gamma_n) = 0$ or Q_{ij}^N , and Q_{ij}^N is the native contact matrix. $Q_{ij}(\Gamma_n) = Q_{ij}^N$ only if residues i and j are located in the same nucleus.

To describe the entropy, first note that besides Γ_1 , each Γ contains an ensemble Γ_0 in which the α_k^a are completely pulled apart (all labels are different). The entropy Δs of unfolded residues in Γ_0 can be estimated from the entropy of unfolded proteins (37), and the entropy cost $\Delta S(\Gamma_n)$ to then sequentially

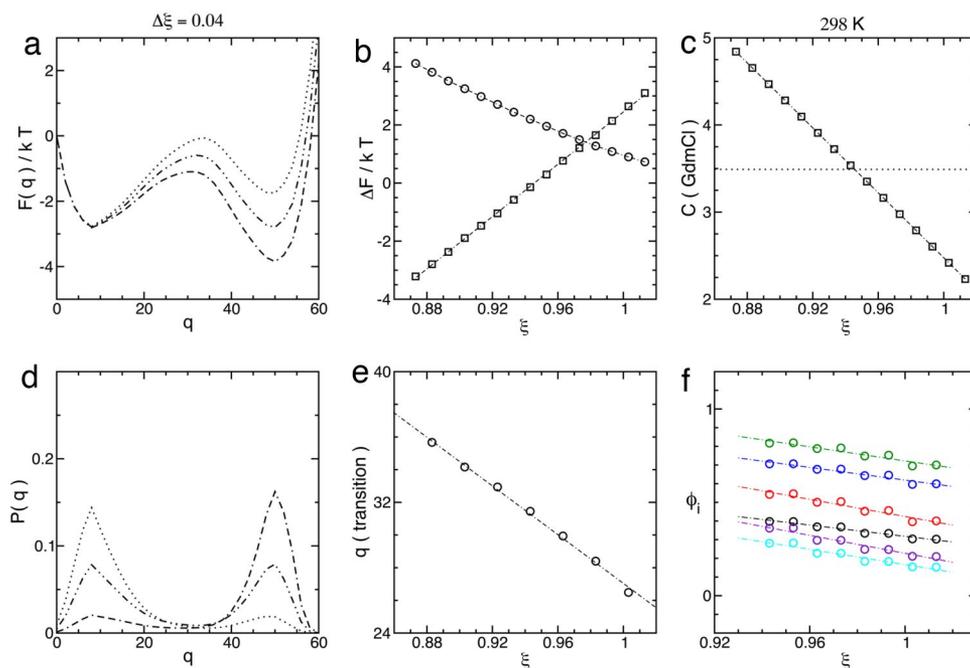


Fig. 2. ξ dependence of landscape parameters. (a) Free energy profile across the melting transition, $\xi_m \approx 0.946$. (b) Melting free energy ΔF_{+D} (\square) and transition state barrier $\Delta F_{\ddagger-D}$ (\circ). (c) Mapping between stability values and denaturant concentration at 25°C. The dotted line indicates the melting concentration $c_m \approx 3.49$ M GdmCl. Data points occur at integer multiples of $\Delta\xi = 0.01$ ($\Delta c \approx 0.186$) about $\xi \approx 0.943$. (d) Distribution of states $P(q)$ corresponding to a. The stability range corresponds to the FRET data in figure 6 of ref. 18. (e) Location of the transition $q^*(\xi)$. The data points were calculated by fitting the barrier to a quadratic. (f) ϕ_i values for the degree of helix formation as in figure 5 of ref. 17 (the color scheme is the same, and the plot describes a similar range of stability). $\phi_i(\xi)$ variations for tertiary structure are slightly larger.

Results

The system can now be depicted as a kind of foam, or network (1) of ensembles with free energy $F(\Gamma_n) = E(\Gamma_n) - TS(\Gamma_n)$, where T is the temperature. To quantitatively compare the model to the data, the melting free energy of the model is mapped to the measured free energy in terms of a stability parameter ξ . To accomplish this, the energy is written as $\varepsilon/T = \xi N \Delta s / Q^N$, where $Q^N = \sum_{i < j} Q_{ij}^N$. The free energy profile is $F(q) = -kT \ln Z(q)$ (Fig. 2a), where $Z(q) = \sum_{\Gamma_n}^q \exp(-F(\Gamma_n)/kT)$ and the sum includes ensembles with q folded residues. The ends of the profile balance when $\xi = 1$.

The profile can be quantified by its critical points in the denatured (D), transition (\ddagger), and native (N) ensembles: The transition barrier is defined as $\Delta F_{\ddagger-D} = F(q^\ddagger) - F(q^D)$ and the melting free energy is $\Delta F_{D-N} = kT \ln Z_D / Z_N$, where $Z_D = \sum_{q \leq q^\ddagger} Z(q)$ and $Z_N = \sum_{q > q^\ddagger} Z(q)$ are the partition functions for denatured and native ensembles (Fig. 2b). ξ is mapped to solvent conditions by equating $\Delta F_{D-N}(\xi)$ to the melting free energy measured at $T = 25^\circ\text{C}$ (17). Fig. 2c plots this relationship and connects the melting point ξ_m to the melting concentration of denaturant. The predicted melting temperature in 2 M guanidinium chloride (GdmCl) is $T_m \approx 50^\circ\text{C}$, very close the value $T_m \approx 52^\circ\text{C}$ measured by Sato and Fersht (17), and the melting transition closely resembles single model FRET data (18) (Fig. 2d). The folding barrier ($\sim 2kT$ at midpoint) has the same order of magnitude as the barrier for an α -carbon model of the protein with G \ddot{o} interactions (42).

The actual size of the barrier can be estimated from chevron plots of folding/unfolding rates versus denaturant (18). Assuming two-state (exponential) kinetics, the slope of the folding arm of the chevron predicts a change of $\sim 7kT$ between 0 M GdmCl and melting, which is not inconsistent with estimates from current kinetic models that include solvent effects explicitly (11, 43). In the kinetic model used by Fersht and coworkers, the slope of the chevron, $m_{\ddagger-D}$, is proportional to the change in solvent-accessible surface area (SASA) between denatured and transition states (18). The fractional change in SASA can be calculated as $m_{\ddagger-D}/m_{D-N} = \partial \Delta G_{\ddagger-D} / \partial \Delta G_{D-N}$, where m_{D-N} is the change in SASA between denatured and native states and G is the Gibbs free energy (10). The result is about $m_{\ddagger-D}/m_{D-N} \sim 0.7$ – 0.8 for BdpA. Although our model does not include solvent, we can calculate $m_{\ddagger-D}/m_{D-N}$ from the ratio of slopes $\Delta \Delta F_{\ddagger-D} / \Delta \Delta F_{D-N}$. The result is $m_{\ddagger-D}/m_{D-N} \approx 0.45$, which is about equal to the fraction of contacts formed at q^\ddagger . Although the model and measured transitions occur in roughly the same regions of the profile (range of native order), a smaller fraction of the surface area is lost in the transition. Because the model is mapped to ΔF_{D-N} this value indicates that the slope of $\Delta F_{\ddagger-D}$ is a bit smaller than in the chevron plots. The difference in scale of activation barriers is very similar to what results when small cooperative (three-particle) terms are added to the G \ddot{o} model (44). These terms can be related to solvent participation in terms of the n -cluster model of phase separation (9, 45), which, along with the results above, suggests that the coupling between the solvent and the structure of the protein (32, 46, 47) is described inaccurately here. It should be possible to account for this coupling better by defining the strength of pair interactions to depend on the amount of local (in space) native order, and the inclusion of these terms already tends to improve protein ϕ values in explicit chain models (44).

In the G \ddot{o} model, ϕ values are usually calculated as $\phi_i \approx Q_{ij}^\ddagger / Q_i^N$, where $Q_i = \sum_j Q_{ij}(\Gamma_n)$ and the angle brackets denote the thermal average at q^\ddagger (48). Fig. 2f plots $\phi_i(\xi)$ for comparison with the $\phi_i(T)$ measurements in ref. 17, and Fig. 2e plots the location of the transition, $q^\ddagger(\xi)$. Variations in $\phi_i(\xi)$ in Fig. 2f roughly agree with the those in $\phi_i(T)$ across the measured temperature range (17), and the uniform increase of curves in Fig. 2f with decreas-

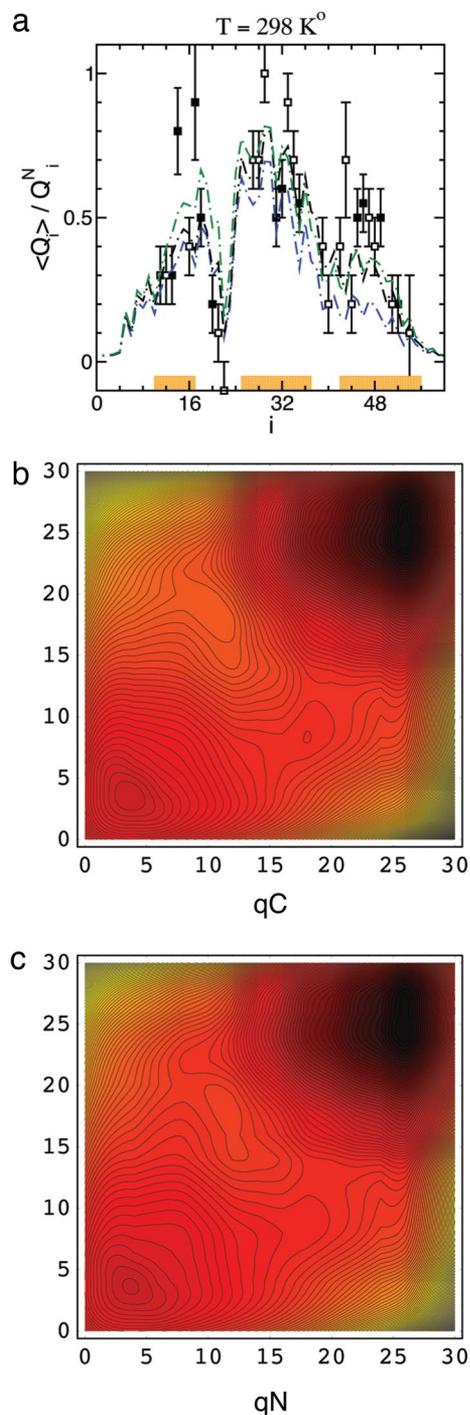


Fig. 4. Two-dimensional projections of the folding network. (a) Calculated ϕ values for the wild-type (blue line) and perturbed (black line) contact matrices are shown together with the wild-type melting values (green line). Measured ϕ values for surface (open symbols) and core (filled symbols) residues are from ref. 16. The level of agreement between the perturbed and measured ϕ values is about the same as in ref. 29. (b and c) Free energy landscapes for two contact models described in *Methods*. The landscapes are a projection of the folding network onto the coordinates $q_N = \sum_{i \leq N/2} q_i$ and $q_C = \sum_{i > N/2} q_i$ where $n = 60$. (b) The wild-type NMR structure. (c) The same structure weighted by the function $(1 + 5/r_{ij})/2$ for ξ corresponding roughly to 2 M GdmCl at 25°C (levels on the landscapes are separated by $\sim 0.1kT$).

ing ξ reflects the slight shift in the transition state toward the native ensemble. Fig. 3 plots the local order, $\langle q_i \rangle$, and the contact order, $\langle Q_{ij} \rangle / Q_{ij}^N$, along the folding profile, and Fig. 4 describes the

